Electronic Structures and Thermoelectric Properties of Two-Dimensional MoS$_2$/MoSe$_2$ Heterostructures

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Thermoelectric properties of bulk and bilayer two-dimensional (2D) MoS$_2$/MoSe$_2$ heterostructures are investigated using density functional theory in conjunction with semiclassical Boltzmann transport theory. It is predicted that the bulk 2D heterostructures could considerably enhance the thermoelectric properties as compared with the bulk MoSe$_2$. The enhancement originates from the reduction in the band gap and the presence of interlayer van der Waals interactions. We therefore propose the 2D MoS$_2$/MoSe$_2$ heterostructures as a possible candidate material for thermoelectric applications.

**Key words:** Heterostructures, Thermoelectric property, Density functional theory, Boltzmann transport theory

I. INTRODUCTION

Thermoelectric materials are considered to have great potential for power generation, energy saving, and environmental protection [1–5]. Various thermoelectric semiconductor materials, such as chalcogenides [6, 7], zintl phases [8], clatharates [9], complex oxides [10], and skutterudites [11, 12] have been developed to convert the waste heat into electricity. The efficiency of thermoelectric device is measured by the material-dependent figure of merit ($ZT=S^2T/\kappa$) [13]. Here, $S$ is the Seebeck coefficient, $\sigma$ is the electrical conductivity, and $\kappa=\kappa_e+\kappa_{lat}$ is the thermal conductivity ($\kappa_e$ and $\kappa_{lat}$ represent the electronic and lattice thermal conductivity contributions, respectively). In general, the figure of merit ($ZT$) can be enhanced by improving the power factor ($S^2\sigma$) or decreasing the thermal conductivity ($\kappa$) of material. The search of materials of high thermoelectric performance is confronted with the challenge that electronic conductivity and Seebeck coefficient have opposite dependencies on the materials parameters: electronic conductivity ($\sigma$) increases as the doping level is improved, but higher doping level leads to lower Seebeck coefficient. Various theoretical and experimental methods have been introduced to enhance the value of $ZT$ [14–26]. For instance, rattler atoms implanted into open structures like clatharates [27] and skutterudites [28] have been introduced to have low-frequency phonons near the acoustic branches, thus enhancing the phonon scattering to reduce the lattice thermal conductivity of the materials.

Two-dimensional (2D) transition-metal dichalcogenide semiconductors such as MoS$_2$ and MoSe$_2$ have significant potential as the ideal thermoelectric materials, since they possess low thermal conductivity along the direction perpendicular to the lattice layers [29–33]. Despite this advantage, $ZT$ values of transition-metal dichalcogenides (TMDCs) are still low due to the difficulty of enhancing the power factor [34–37]. To solve this problem, we propose the use of 2D heterostructures systems such as MoS$_2$/MoSe$_2$, which are formed by stacking two different TMDCs layers together. Based on density functional theory (DFT) calculations, we demonstrate that such 2D heterostructures materials possess many improved thermoelectric properties as compared with their parental pristine materials.

II. COMPUTATIONAL METHODS

First-principles calculations of bulk and bilayer MoS$_2$/MoSe$_2$ 2D heterostructures system are conducted using DFT methods implemented in the Vienna ab initio simulation package (VASP) [38]. The projector-augmented-wave pseudopotentials and the generalized gradient approximation of Perdew, Burke, and Ernzerhof (PBE) for exchange-correlation functional are adopted in our simulations [39]. Furthermore, van der Waals interactions are taken into account by us-
ing the semiempirical correction of Grimme (DFT-D3) [40]. The energy cutoff for a plane-wave expansion is set to 500 eV. All atomic coordinates are relaxed until the atomic forces have declined to 0.01 eV/Å, enforcing a total energy convergence criterion of $1 \times 10^{-5}$ eV. A vacuum slab larger than 15 Å is added to avoid interaction between adjacent images of the bilayer structure.

Temperature- and doping-dependent electronic transport properties, including electronic conductivity and Seebeck coefficient, are computed by using the semi-classical Boltzmann transport theory [41, 42]. The constant scattering time approximation is adopted, which is valid if the electron relaxation time does not vary strongly with the energy on a scale of $k_B T$, and the rigid band approaches as implemented in the BoltzTraP code [43]. By using a Fourier expansion [44, 45], while maintaining the crystal symmetry [46], the BoltzTrap code fits the ab initio electronic band structure to an analytic function. Since the transport properties can be very sensitive to the Brillouin zone (BZ) sampling, especially for low doping levels and low temperatures, we calculate the electronic structures required for the transport calculations with very dense $k$-meshes (43\times43\times11 for the hexagonal BZ of bulk 2D heterostructures, and 43\times43\times5 for the trigonal BZ of the bilayer structure).

The temperature-dependent and doping-level-dependent thermoelectric transport tensors, such as electronic conductivity $\sigma_{\alpha\beta}(T, \mu)$, Seebeck coefficient $S_{\alpha\beta}(T, \mu)$, and thermal conductivity (electronic part $\kappa_{\alpha\beta}^{el}(T, \mu)$) tensors are calculated as follows [43]:

\[
\sigma_{\alpha\beta}(T, \mu) = \frac{1}{\Omega} \int \sigma_{\alpha\beta}(\varepsilon) \left[ \frac{\partial f_0(T, \varepsilon, \mu)}{\partial \varepsilon} \right] \, d\varepsilon \quad (1)
\]

\[
S_{\alpha\beta}(T, \mu) = \frac{1}{e T \Omega \sigma_{\alpha\beta}(T, \mu)} \int \sigma_{\alpha\beta}(\varepsilon - \mu) \left[ \frac{\partial f_0(T, \varepsilon, \mu)}{\partial \varepsilon} \right] \, d\varepsilon \quad (2)
\]

\[
\kappa_{\alpha\beta}^{el}(T, \mu) = \frac{1}{e^2 T \Omega \sigma_{\alpha\beta}(T, \mu)} \int \sigma_{\alpha\beta}(\varepsilon - \mu)^2 \left[ \frac{\partial f_0(T, \varepsilon, \mu)}{\partial \varepsilon} \right] \, d\varepsilon \quad (3)
\]

Here, $\alpha$ and $\beta$ are the tensor indices, $\Omega$ is the volume of the unit cell, $\varepsilon$ is the charge of the electron, $f_0(T, \varepsilon, \mu)$ is the Fermi distribution function, and $\mu$ is the Fermi level. The conductivity tensor $\sigma_{\alpha\beta}(\varepsilon)$ (transport distributions) can be expressed analytically as [43]:

\[
\sigma_{\alpha\beta}(\varepsilon) = \frac{1}{N} \sum_{i,k} \sigma_{\alpha\beta}(i, k) \delta(\varepsilon - \varepsilon_{i,k}) \quad (4)
\]

which can be expressed using $k$-dependent conductivity tensor as [43]:

\[
\sigma_{\alpha\beta}(i, k) = e^2 \tau_{i,k} \nu_{\alpha}(i, k) \nu_{\beta}(i, k) \quad (5)
\]

where $i$ is the band index, $k$ is the reciprocal vector, $N$ is a normalization depending on the number of $k$ points sampled in the BZ, $\tau_{i,k}$ is the electronic relaxation time, and $\nu_{\alpha}(i, k)$ is the $i$ component of band velocity $\nabla_{k,\varepsilon}(k)$ with $\varepsilon$ being the band energies. As demonstrated in the above formula, temperature-dependent transport properties can be calculated from the Fermi distribution function, and one can achieve the doping-level dependent transport properties by adjusting the Fermi level $\mu$ which is directly associated with doping concentration [43].

The electron relaxation time $\tau$ characterizing the average time between two consecutive electron scattering events is a crucial parameter for calculating the thermoelectric properties, such as the electrical conductivity ($\sigma$) and the electronic thermal conductivity ($\kappa_{e}$), since just the ratio of these conductivity to the relaxation time ($\sigma/\tau$ and $\kappa_{e}/\tau$) can be achieved by using the BoltzTraP code. The value of $\tau$ is usually obtained by fitting the calculated ratio of $\sigma/\tau$ to measure electrical conductivity data. However, such experimental data for the MoS$_2$/MoSe$_2$ 2D heterostructures have so far remained unavailable. Therefore, in this work we focus on the ratio of thermal properties to the electron relaxation time rather than on the properties themselves.

III. RESULTS AND DISCUSSION

A. Crystal structure

The monolayer structure of MoS$_2$ and MoSe$_2$, consists of a single (S/Se)-Mo-(S/Se) layer with space group P6$_3$mc (187), which has no inversion symmetry. While the bulk MoS$_2$ and MoSe$_2$ has a 2H-polytype structure in the P6$_3$mc space group (194). Its supercell consists of two (S/Se)-Mo-(S/Se) layers separated along the $z$ axis, and the two layers are bound by van der Waals interactions. Furthermore, due to the increasing radius of the chalcogen atoms, the optimized values of lattice constants for monolayer along in-plane direction increase from $a=3.162$ Å in MoS$_2$ to 3.320 Å in MoSe$_2$. In general the lattice mismatch may lead to stacking disorder or Moiré Pattern superstructures. However, the intrinsic lattice mismatch between the layer of MoS$_2$ and MoSe$_2$ is as small as 0.158 Å. Moreover, the explicit consideration of such a small lattice mismatch would require the use of very large supercell and thus make the calculation rather expensive. Therefore, in our simulations for the 2D heterostructures, the same lattice constant is adopted for the both types of layers (MoS$_2$ and MoSe$_2$).

The optimized MoS$_2$/MoSe$_2$ 2D heterostructures for bulk system in our calculation has the lattice parameter of $a=3.248$ and 3.250 Å for bilayer, which is consistent with the other theoretical results [47–49]. As in Fig.1, the Mo atoms of MoSe$_2$ monolayer sit on the top of the chalcogen atoms S of MoS$_2$ monolayer, and those monolayer which constructs the heterostructures shows a lateral shift. Due to the van der Waals binding, the Mo

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B. Electronic structure

Electronic band structures and DOS for bulk and bilayer MoS$_2$/MoSe$_2$ 2D heterostructures are presented in Fig.2. For the bulk 2D heterostructures, as demonstrated in Fig.2(a), an indirect band gap of 0.546 eV is observed with the valence band maximum at the Γ point and the conduction band minimum at the K point, which is consistent with the theoretical results reported by Changhoon et al. [47]. The electronic band structure along high symmetry point of in-plane and cross-plane direction shows a great anisotropy due to the 2D heterostructures constructed by van der Waals binding, and the band gap of the in-plane bands (Γ-M-K-Γ) is much smaller than cross-plane one (Γ-A). Bilayer 2D heterostructures, on the other hand, also show an indirect band gap of 0.695 eV with both the valence band maximum at the Γ point and conduction band minimum at the high symmetry K point, which is consistent with other theoretical results [49]. Furthermore, both the bulk and bilayer systems show a strong asymmetric feature between the valence and conduction bands. Although GGA-PBE is known to underestimate band gaps of semiconductors, the resulting electronic structure are considered to be reasonably accurate for subsequent computation of thermoelectric properties.

C. Thermoelectric properties

To enlarge $ZT$, the material should have a larger power factor $S^2\sigma$ and smaller $\kappa (=\kappa_e+\kappa_{lat})$. Figure 3 depict the in-plane and cross-plane power factor divided by the relaxation time $\tau$, $S^2\sigma/\tau$, of the bulk MoS$_2$/MoSe$_2$ heterostructures under doping (both p- and n-type), with the temperature ranging from 300 K to 1200 K. Here, $\tau$ is the relaxation time that is not directly determined by the band structure, but depends on the temperature, the doping level, and also the sample details (such as defect types and concentrations) [43]. Note that we compare $S^2\sigma/\tau$ instead of $S^2\sigma$, because the relaxation time is difficult to calculate and the electronic conductivity has not been measured experimentally. As demonstrated in Fig.3, $S^2\sigma/\tau$ is enhanced as the carrier concentration increases at each temperature. Its maximum value is nearly within the carrier concentration range of $10^{20}-10^{21}$ cm$^{-3}$ for each temperature, which also implies that high carrier concentration could enhance the power factor. As shown in Fig.3, for bulk heterostructures, the p-type doping at in-plane direction shows the largest power factor $S^2\sigma/\tau$ at temperature 1200 K. To better reflect the thermoelectric performance of bulk 2D MoS$_2$/MoSe$_2$ heterostructures, the theoretical results of pristine bulk MoSe$_2$ at the hole carrier concentration of $5\times10^{20}$ cm$^{-3}$ are adopted [36]. As demonstrated in Table I, although the pristine MoSe$_2$ shows a slightly higher $S^2\sigma/\tau$ at 1200 K,
FIG. 3 In-plane (a, c) and cross-plane (b, d) temperature-dependent power factor divided by the scattering time (PF/τ) as a function of p- and n-type doping concentration for bulk MoS$_2$/MoSe$_2$ 2D heterostructures.

TABLE I Temperature dependent power factor divided with relaxation time ($S^2σ/τ$) for bulk MoSe$_2$ and MoS$_2$/MoSe$_2$ 2D heterostructures along the in-plane direction at the hole carrier concentration of 5×10$^{20}$ cm$^{-3}$.

<table>
<thead>
<tr>
<th>T/K</th>
<th>(S$^2σ/τ$)/(10$^{11}$ Wm$^{-1}$K$^{-2}$s$^{-1}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>MoS$_2$/MoSe$_2$</td>
</tr>
<tr>
<td>300</td>
<td>1.23</td>
</tr>
<tr>
<td>600</td>
<td>3.10</td>
</tr>
<tr>
<td>900</td>
<td>4.84</td>
</tr>
<tr>
<td>1200</td>
<td>6.02</td>
</tr>
</tbody>
</table>

the bulk MoS$_2$/MoSe$_2$ heterostructures shows an overall better thermoelectric performance along the in-plane direction. Despite the difference in relaxation time between these two crystals, such a comparison provides an overall assessment for their thermoelectric performances.

Along the cross-plane direction, the n-type doping shows a greater power factor $S^2σ/τ$ than p-type one. However, since in TMDCs the relaxation time of in-plane direction is two orders of magnitude larger than the cross-plane one [36, 37], the in-plane electrical conductivity is typically two orders magnitude larger than the cross-plane electrical conductivity. Then, the power factor along in-plane direction is expected to be two orders of magnitude larger than the cross-plane counterpart, since both of them have similar Seebeck coefficient values. Additionally, the DOS close to the valence band edge is much larger than those near the conduction band edge, which suggests that p-type doping could have a better thermoelectric performance [50]. Therefore, we will focus on the p-type doping bulk heterostructures, and discuss the temperature-dependent and doping-level-dependent Seebeck coefficient, the electric conductivity and the thermal conductivity individually.

The p-type doping in-plane and cross-plane Seebeck coefficients as functions of carrier concentration are shown in Fig.4 (a) and (b). Similar to the other TMDCs [36, 37], the bulk 2D heterostructures has a large Seebeck coefficient. At a fixed carrier concentration, for both in-plane and cross-plane directions, the Seebeck coefficient of bulk 2D heterostructures slightly increases as the temperature is increasing. This phenomenon mainly originates from the Fermi broadening as the temperature rises, and then it leads to an increasing effective density of states at the top of valence band [51]. Consistent with the known thermoelectric behavior for the other TMDCs [36, 37], the maximum value of Seebeck coefficient for each temperature shifts to high doping level and decrease as temperature is increased for both cross- and in-plane direction. The calculated tiny band gap for bulk 2D heterostructures (0.546 eV),
FIG. 4 In-plane (a, c, e) and cross-plane (b, d, f) temperature- and p-type doping concentration-dependent Seebeck coefficient, electronic conductivity divided by the scattering time ($\sigma/\tau$), and electronic thermal conductivity divided by the scattering time ($\kappa_e/\tau$) of bulk MoS$_2$/MoSe$_2$ heterostructures, respectively.

as mentioned above, likely lead to the bipolar effect at low doping carrier concentration which make the Seebeck coefficient decreases with decreasing doping concentration, opposite to the usual situation [52]. As temperature is higher than 900 K, the Seebeck coefficient along the in-plane direction presents a sign reversal at low doping level, which is attributed to the increasing negative contribution of thermally excited electrons to the Seebeck coefficient under the bipolar-transport conditions [53]. While the Seebeck coefficient along the cross-plane direction does not show a sign reversal and more stable with the doping concentration increasing at low doping level, indicating that the system along cross-plane direction shows a weak bipolar effect originated by the large band gap along this direction. This anisotropy can also be observed by the electrical conductivity divided by the relaxation time ($\sigma/\tau$) as a function of doping concentration. As demonstrated in Fig.4 (c) and (d), the conductivity divided by the relaxation time ($\sigma/\tau$) of in-plane is about one order higher than the cross-plane one, revealing that the thermally excited carrier concentration along the in-plane direction is significantly higher than cross-plane one. Furthermore, in the 900–1200 K temperature range, the electrical conductivity divided by the relaxation time ($\sigma/\tau$) does not depend strongly on the doping concentration at low doping level, since the thermally excited carriers dominate transport [53]. To overcome the contribution by the thermally excited carrier concentration, the higher doping concentration is required as temperature is higher. As the doping concentration above the onset of bipolar transport, the electrical conductivity divided by the relaxation time ($\sigma/\tau$) increases substantially with the increasing doping concentration.

The electronic band structure also supports this viewpoint, as the band gap of in-plane (along high symmetry point $\Gamma$-M-K-$\Gamma$) is much smaller than the cross-plane one ($\Gamma$-A). The electrical thermal conductivities divided by the relaxation time ($\kappa_e/\tau$) along the in-plane and cross-plane directions are depicted in Fig.4 (e) and (f), respectively. Although the electronic contribution to the thermal conductivity is small, compared with the lattice thermal conductivity, the electronic thermal conductivity also illustrates the anisotropy of thermal conductivity between cross-plane and in-plane. The power factor of in-plane is considerably larger than the cross-plane one, especially since the relaxation time of cross-plane is much smaller than the in-plane one. Furthermore, the electronic thermal conductivity divided by the relaxation time ($\kappa_e/\tau$) at a fixed carrier concentrations for both in-plane and cross-plane increases as temperature rising, mainly because of more intense electron scattering as temperature increasing. According to the Wiedemann-Franz law [43],

$$\kappa_{e\alpha\beta} = \frac{\pi^2}{3} \left( \frac{k_B}{e} \right)^2 \sigma_{\alpha\beta} T$$

the electronic thermal conductivity is proportional to the temperature of system. Meanwhile, since thermal conductivity is proportional to the electronic conductivity that is highly anisotropic, there is a significant

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FIG. 5 Temperature-dependent power factor divided by the scattering time (PF/τ) of bilayer MoS$_2$/MoSe$_2$ 2D heterostructures as function of n- and p-type doping concentration.

FIG. 6 Temperature dependent Seebeck coefficient (a, b), electronic conductivity divided by the scattering time (σ/τ) (c, d), and electronic thermal conductivity divided by the scattering time (κ/τ) (e, f) of bilayer MoS$_2$/MoSe$_2$ heterostructures as a function of n- and p-type doping concentration, respectively.

difference between the in-plane and cross-plane components.

Compared with the bulk heterostructures, the bilayer heterostructures show a much lower power factor (S$^2$σ/τ) as demonstrated in Fig.5. Since the band gap of bilayer 2D heterostructures is larger than that of the bulk, the electronic conductivity of bilayer heterostructures is much smaller than that of the bulk, see Fig.6 (a) and (b). Furthermore, since the bulk and bilayer heterostructures have similar Seebeck coefficients, as demonstrated in Fig.6 (c) and (d), the bulk heterostructures should have a better thermoelectric performance than those of bilayer one. While the electrical thermal conductivity is smaller than the bulk one, as presented in Fig.6 (e) and (f). For p-type doping, the bilayer heterostructures show a similar thermoelectric performance to the monolayer one [36].

IV. CONCLUSION

Based on the electrical band structure calculated from first principles, the thermoelectric properties of bulk and bilayer 2D MoS$_2$/MoSe$_2$ heterostructures have been analyzed by using the semi-classical Boltzmann transport theory. Both n-type and p-type doping have been addressed for bulk and bilayer heterostructures, employing the rigid band approximation and constant scattering time approximation. Due to a smaller band gap and more dense DOS close to the valence band edge

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than those near the conduction band edge, the thermoelectric performance of bulk 2D MoS$_2$/MoSe$_2$ heterostructures turns out to be superior to pristine bulk MoSe$_2$ along the in-plane direction for p-type doping at a wide temperature range. Furthermore, with a larger band gap, the bilayer heterostructures show a much lower electronic conductivity than those of bulk heterostructures, which also induces that it shows a weaker thermoelectric performance than bulk one. Although the power factor of bilayer heterostructures is lower than those of bulk heterostructures, it shows a similar thermoelectric performance to the monolayer MoSe$_2$ for p-type doping at each temperature. Therefore, we safely conclude that such 2D heterostructures materials possess much improved thermoelectric properties as compared with their parental pristine materials, especially for bulk one. As reported by Li et al. [54], the thermal lattice conductivity considered the spin-orbit coupling (SOC) effect is higher than those value not considered. Furthermore, the band shape and the band gap which make a great influence on the calculation of thermoelectric properties could be changed as the SOC effect is introduced, thus the SOC effect should be taken into account. However, the SOC is not considered in the present work, because of the limited computational resources at our disposal. The influence of the SOC on the thermoelectric properties is to be addressed in our future work.

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